

Homework 7 - due Wednesday, August 9 at 10:00AM

Diagonalization and Orthogonal Projection Practice

Make sure to justify your solution for each problem.

1. Let $A = \begin{bmatrix} 2 & 3 \\ 0 & -1 \end{bmatrix}$. Diagonalize A , then find a formula for A^k .

2. Let $\mathbf{y} = \begin{bmatrix} 6 \\ 3 \\ -2 \end{bmatrix}$, $\mathbf{u}_1 = \begin{bmatrix} 3 \\ 4 \\ 0 \end{bmatrix}$, and $\mathbf{u}_2 = \begin{bmatrix} -4 \\ 3 \\ 0 \end{bmatrix}$.

(a) Verify that $\{\mathbf{u}_1, \mathbf{u}_2\}$ is an orthogonal set.

(b) Find the orthogonal projection of \mathbf{y} onto $\text{Span}\{\mathbf{u}_1, \mathbf{u}_2\}$.